Adaptive Type-2 Fuzzy Sliding Mode Control for Grid-Connected Wind Turbine Generator Using Very Sparse Matrix Converter

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Abstract-The strategy to improve both efficiency and power quality of grid-connected wind turbine generator systems (WTGs) are presented. WTGs efficiency is improved by developing a variable speed control to obtain maximum power at all wind speeds. Variable speed control based on Adaptive Type-2 Fuzzy Sliding Mode Control (AFSMOC) is proposed by employing Very Sparse Matrix Converter (VSMC). Type-2 fuzzy system is used to improve the robustness of sliding mode control. VSMC can provide low harmonics in line current, so the power quality problems can be minimized. The simulation results shows that the AFSMOC can regulate the generator speed at optimum Tip Speed Ratio (TSR) with maximum error 2.5 rpm, so that the maximum power can be obtained at all wind speeds. VSMC also provide good performance with Total Harmonic Distortion (THD) of voltage 0.35% and THD of current 6.82%.

Keywords-Wind turbine generator; very sparse matrix converter; adaptive type-2 fuzzy sliding mode control; variable speed control.

1. Introduction

The Wind turbine generator system (WTGs) is one of the ways to deal with the growing electric energy demands in Indonesia. WTGs widely developed with variable speed operation because it can increase the efficiency with maximum output power and widen the operating range at all wind speeds [1,2]. Variable speed WTGs many uses Permanent Magnet Synchronous Generator (PMSG) due many advantages such as self excitation, easy to control, smaller in size, and has a high efficiency with the absence of rotor losses [3,4].

Generally, variable speed control of WTGs using power converter. Various types of converters have been applied to WTGs. Converter types widely used for PMSG-wind turbine are back to back converter, dioda rectifier-inverter and matrix converter [5,6]. Multilevel inverter also been applied to improve the voltage quality of WTGs [7]. Matrix converter is the best alternative to the grid-connected WTGs because higher efficiency with increased power density, not dc-link storage and low THD in line current [8,9]. One of the disadvantages of conventional matrix converter is using a lot of switches, so it becomes expensive. To resolve this problem has developed several models of sparse matrix converter [10,11], and one of the models that have been used for WTGs is VSMC [12].

In this paper, variable speed control of grid-connected PMSG-wind turbine is proposed by using VSMC. The PMSG speed is controlled at optimum point of TSR to obtain maximum power at all wind speeds. The PMSG speed control many developed by Field Oriented Control (FOC). This method is applied with decoupled control of torque and flux through the stator current in direct-quadrature axis \((i_d, i_q)\). Several control strategies have been implemented for
FOC, One is Sliding Mode Control (SMC) [13,14]. SMC has received much attention due robust to disturbances [13].

To improve the robustness, SMC can be developed with adaptive gain. Wavelet neural network and extended state observer for adaptive gain of SMC has been discussed in [13,14]. In this paper, adaptive gain of SMC is proposed by using type-2 fuzzy system (T2FS). It is more attractive to handle the uncertainty of membership function parameters, so that the adaptive gain becomes more valid to improve the SMC performances [15,16]. It will improve the performance of variable speed control of grid-connected PMSG-wind turbine.

2. Wind Turbine Generator System Modeling

The proposed variable speed control of grid-connected PMSG-wind turbine is shown in Fig. 1. The proposed system consists of horizontal wind turbine, PMSG connected to the grid through VSMC, resistive load and speed controller. Small LC filter is placed on the grid side to improve the quality of both the voltage and current. The speed controller is developed by using FOC method based on constant torque angle control. In this method, decoupled control of torque and flux is adopted to adjust the stator current in direct-quadrature axis (i_d,i_q). AFSMOC is applied to obtain the reference of q-axis stator current i^*_q based on speed error, while the reference of d-axis stator current i^*_d is kept zero. To obtain the reference voltage (v^*_d and v^*_q) for modulate a VSMC, both i^*_d and i^*_q are regulated by SMC.

2.1. Permanent Magnet Synchronous Generator Modeling

The dynamic model of Permanent Magnet Synchronous Generator (PMSG) for variable speed control in FOC method are projected in dq-axis of rotating synchronous reference frame. In this scheme, the dq-axis stator current (i_d and i_q) can be written as:

\[
\frac{d}{dt} \begin{bmatrix} i_d \\ i_q \end{bmatrix} = \begin{bmatrix} \frac{-R_s}{L_d} & \frac{\omega_e}{L_d} \\ -\omega_e & \frac{-R_s}{L_q} \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} + \begin{bmatrix} \frac{v_d}{L_d} \\ \frac{v_q}{L_q} - \omega_e \psi_m \end{bmatrix}
\]  

(1)

where R_s, \omega_e, n_p, and \psi_m are the stator resistance, the electrical speed, the number of pole pairs and the flux of permanent magnet, respectively. L_d, L_q, and v_d,v_q are the stator inductances and the stator voltages in dq-axis, respectively.

PMSG speed control using AFSMOC is applied by regulating the electromagnetic torque \(T_e\) through q-axis stator current \(i^*_q\) control based on the mechanical dynamic of PMSG, as in Eq. (2). The relationship between \(T_e\) and \(i_q\) is expressed in Eq. (3).

\[
\frac{d}{dt} \omega_m = \frac{T_m - T_e - B \omega_m}{J}
\]

(2)

\[
T_e = -1.5 n_p \psi m i^*_q
\]

(3)

where \(\omega_m, T_m, B\) and \(J\) are the mechanical speed, the electromagnetic torque, the mechanical torque, the friction coefficient and the inertia moment, respectively. The output power of PMSG \(P_s\) is:

\[
P_s = \frac{3}{2} \left( v_d i_d + v_q i_q \right)
\]

(4)

2.2. Very Sparse Matrix Converter Modeling

Very Sparse Matrix Converter (VSMC) is one type of indirect matrix converter which uses 12 active switches. The structure of VSMC can be seen in Fig. 1.

![Fig. 1. The structure of variable speed control the PMSG wind turbine](image-url)
This type less expensive than conventional indirect matrix converter which uses 18 active switches. The main difference between direct matrix converter with indirect matrix converter is in the switches structure. The direct matrix converter switches arranged in a matrix form, whereas the indirect matrix converter switches is organized into two groups converter as a back-to-back converter, so that the modulation strategies of indirect matrix converter easier than direct matrix converter.

VSMC consists of the current source converters (CSC) and the voltage source converters (VSC) as shown in Fig.1. The advantages of VSMC is not using the DC-link energy storage that require large size capacitor. As a replacement, small LC filter is employed to reduce the input harmonics. In this paper, VSMC is modulated by using Space vector modulation.

The modulation strategy of the CSC switches is to generate the maximum dc-link voltage and keep unity input power factor. The switching states of CSC are determined based on the space vector of the input voltages that are divided into 6 sectors, as shown in Fig. 2a. The duty cycle of the CSC switches in \( \alpha \beta \) for sector 1 are:

\[
\begin{align*}
    d_{\alpha} &= -\left( \frac{i_b}{i_a} \right) = -\left( \frac{v_b}{v_a} \right) \\
    d_{\beta} &= -\left( \frac{i_c}{i_a} \right) = -\left( \frac{v_c}{v_a} \right) \\
    d_{\alpha} + d_{\beta} &= 1
\end{align*}
\]  

(5)

The duty cycle of CSC switches for each sector can be calculated based on Eq. (5) and the space vector of the input voltage in Fig. 2a.

The VSC switches are modulated based on space vector of the output voltages, that are separated by 6 sectors as shown in Fig. 2b. The duty cycle of the VSC switches are:

\[
\begin{align*}
    d_{\alpha_0} &= m_o \sin \left( \frac{\pi}{3} - \theta_o \right) \\
    d_{\beta_o} &= m_o \sin \left( \frac{\pi}{3} \right) \\
    d_{\beta_0} &= 1 - d_{\alpha_0} - d_{\beta_0}
\end{align*}
\]  

(6)

where \( m_o = 4V_o/3V_i \) is modulation index. \( \theta_o, V_o \) and \( V_i \) are the output voltage angle, the output voltage amplitude and the input voltage amplitude, respectively.

To balance the input currents and the output voltages, the CSC switches must be coordinated with the VSC switches. Note that the states change of the CSC switches always occurs during free-wheeling condition of the VSC switches. Fig. 3 shows the coordination between the CSC switches with the VSC switches for sector 1.

The modulation pulses are achieved by compare the switching time with linear carrier pulse.

\[
\begin{align*}
    T_1 &= T_{12} = 0.5 \cdot d_{\beta_0} \cdot d_{\alpha_0}, \quad T_4 = T_9 = 0.5 \cdot d_{\alpha_1} \cdot d_{\beta_0} \\
    T_2 &= T_{11} = 0.5 \cdot d_{\beta_0} \cdot d_{\beta_0}, \quad T_5 = T_6 = 0.5 \cdot d_{\alpha_1} \cdot d_{\beta_0} \\
    T_3 &= T_{10} = 0.5 \cdot d_{\beta_0} \cdot d_{\beta_0}, \quad T_8 = T_7 = 0.5 \cdot d_{\alpha_1} \cdot d_{\beta_0} \\
    T_s &= T_1 + T_2 + \ldots + T_{12} = 1
\end{align*}
\]  

(7)
2.2.2.3 Wind Turbine Modeling

Based on the aerodynamic characteristics, the mechanical power available from a wind turbine $P_m$ to drive PMSG can be written as:

$$P_m = 0.5 \pi R^2 C_p \left( \frac{\omega_m}{R} \right) \rho v_w^3$$

(8)

where $\rho$ is the air density, $R$ is the blade radius, $v_w$ is the wind speed and $C_p$ is power coefficient of turbine, which is a function of the tip speed ratio (TSR) $\lambda$ and the pitch angle $\beta$. TSR depends on the rotor speed, which can be written as:

$$\lambda = \frac{\omega_m R}{v_w}$$

(9)

Based on Eq. (8) and (9), the mechanical power $P_m$ of wind turbine also depends on the rotor speed $\omega_m$. Figure 4 shows the mechanical power curve versus rotor speed. For each wind speed, there exists a maximum power point. Wind turbine can achieve the maximum power point $P_{m\text{, max}}$ when operating at maximum power coefficient $C_{p\text{, max}}$ and optimum TSR $\lambda_{opt}$ [17], which is written as:

$$P_{m\text{, max}} = 0.5 \pi R^2 \rho C_{p\text{, max}} \left( \lambda_{opt} \right) \beta v_w^3$$

(10)

Fig. 4. The mechanical power curve of wind turbine

Variation of wind speed generates maximum power point located at different rotor speeds, as shown in Fig. 4. The reference speed $\omega_{m*}$ for maximum power is given by:

$$\omega_{m*} = v_w \frac{\lambda_{opt}}{R}$$

(11)

To obtain maximum power at all wind speed, variable speed control is required to maintain the wind turbine operation at optimum TSR. In this paper, variable speed control of PMSG wind turbine is proposed using AFSMOC.

3. PMSG Speed Control Based on AFSMOC

Variable speed control of PMSG is proposed by using Adaptive Type-2 Fuzzy Sliding Mode Control (AFSMOC) based on Field oriented control. In this method, the PMSG speed is controlled by regulating the electromagnetic torque through $q$-axis stator current control, while the $d$-axis stator current is kept zero. AFSMOC is applied to regulate the reference of $q$-axis stator current $i_{q*}$ based on speed error $e_{w}$.

Figure 5 shows the structure of AFMOC for PMSG speed control.

![Fig. 5. The structure of AFMOC.](image)

The structure of AFMOC consists of the sliding surface stage, the adaptive gain stage and the control law stage. T2FS is applied to obtain the adaptive gain $G_s$, so that the robustness of speed controller can be improved.

PMSG speed control using AFMOC is developed from mechanical dynamic of PMSG in Eq. (2). The mechanical dynamics of PMSG with parameter variations due system disturbances can be formulated from Eq. (2) and Eq. (3) as follows:

$$\frac{d}{dt} \omega_m = \left( 1.5 n_p \psi_m \dot{i}_q + J \right) + K_i$$

(12)

$$K_i = \left( T_m - 1.5 n_p \psi_m \left( i_{q*} - i_q \right) - B \omega_m \right) / J$$

(13)

where $K_i$ is the lumped disturbances of system. The control law of AFMOC to obtain $i_{q*}$ is given by:

$$i_{q*} = K_i e_{w*} + G_s \text{sat} \left( \frac{S}{\phi} \right) + \left( \frac{d}{dt} \omega_m A^{-1} \right)$$

(14)

with

$$e_w = \omega_{w*} - \omega_m$$

(15)

where $G_s$ is adaptive gain obtained from T2FS, $\omega_{w*}$ is the measured speed, $\omega_m$ is the reference speed obtained from Eq. (11), $K_i$ is the speed error gain and $S$ is the sliding surface which is given by:

$$S = e_{w*} + A K_s \int_0^t e_w \, dt$$

(16)

with saturation function of sliding surface:

$$\text{sat} \left( \frac{S}{\phi} \right) = \begin{cases} 1 & S > \phi \\ \frac{S}{\phi} - \phi < S < \phi \\ -1 & S < -\phi \end{cases}$$

(17)

Where $\phi$ is a constant. The AFMOC performances are determined by $K_i$ and $G_s$. It is verified using Lyapunov function. Assume that the lumped disturbances of system in Eq. (13) satisfies $0 \leq |K_i| < \delta$. Using Eq. (14), the speed error converges to zero if $G_s > A^\phi \delta$. If the Lyapunov function is
defined as $V = 0.5 \, S^2$, the derivative of the Lyapunov function can be formulated by using Eq. (14) as follow:

$$\frac{d}{dt} V = \frac{d}{dt} S = S \left( \frac{d}{dt} e_{\omega} + A \, K_e \, e_{\omega} \right)$$

$$= -A S \left( i_q + A^{-1} K_i - K_e \, e_{\omega} - A^{-1} \frac{d}{dt} \omega_m \right)$$

$$= -A \left( G_s |S| + A^{-1} S \, K_i \right)$$

$$\leq -A |S| \left( G_s - A^{-1} \, h \right) < 0 \quad (S \neq 0) \quad (18)$$

The theorem is proved if Eq. (14) makes Eq. (16) converge to zero.

3.1. Type-2 Fuzzy System

Type-2 Fuzzy System (T2FS) is used to obtain the adaptive gain of AFSMOC ($G_s$) with inputs the sliding surface $s = S \, K_i$ and its derivatives of sliding surface $d_s = S \, K_{\omega_m}$, where $K_{\omega_m}$ is the T2FS input gain.

The T2FS structure consists of fuzzifier, rule base, fuzzy inference engine, type-reducer and defuzzifier [15,16]. In fuzzifier, the input values are mapping into the membership function, which is presented by upper membership function and lower membership function. The interval between these two function represent the footprint of uncertainty (FOU), which is used to characterize a type-2 fuzzy set. Triangular membership function with uncertain width is used in this paper, as shown in Fig. 6.

The firing strength of the $i$-th rule can be expressed as:

$$F^i = \left[ f^i \bar{f}^i \right] \quad (21)$$

$$f^i = \mu_{X_i} (s) \times \mu_{X_{di}} (ds) \quad \text{and} \quad \bar{f}^i = \bar{\mu}_{X_i} (s) \times \bar{\mu}_{X_{di}} (ds) \quad (22)$$

where $\mu$ and $\bar{\mu}$ denote the lower membership function and the upper membership function, respectively. Using the center of set (COS) type-reduction, the output fuzzy T2FS can be written as:

$$Y_{\text{COS}} = [y_l, y_r] \quad (23)$$

where $Y_{\text{COS}}$ is an interval type-1 set, $y_l$ and $y_r$ are the left end point or the minimum value of $y$ and the right end point or the maximum value of $y$, respectively. $y_l$ and $y_r$ can be computed using the Karnik-Mendel algorithm as follows:

$$y_l = \frac{\sum_{i=1}^{L} f^i \, w^i_l + \sum_{i=L+1}^{M} f^i \, w^i \, \bar{f}^i}{\sum_{i=1}^{L} f^i + \sum_{i=L+1}^{M} f^i \, \bar{f}^i} \quad (24)$$

$$y_r = \frac{\sum_{i=1}^{R} f^i \, w^i + \sum_{i=R+1}^{M} \bar{f}^i \, \bar{w}^i \, \bar{f}^i}{\sum_{i=1}^{R} f^i + \sum_{i=R+1}^{M} \bar{f}^i \, \bar{w}^i \, \bar{f}^i} \quad (25)$$

where $w_l$, $w_r$ are the consequent centroid set with interval ($i = 1, \ldots, M$), while $M$ is the total number of rules in the rule base of a T2FS. The adaptive gain of AFSMOC $G_s$ is obtained from the defuzzified crisp output as follows:

Table 1. Rule base of T2FS

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Fig. 6. Membership function of T2FS. (a) the input $s$, (b) the input $d_s$, (c) the output $G_s$. The $i$-th T2FS rules can be written as:

$$R^i = \text{IF } s \text{ is } X_i^l \text{ and } d_s \text{ is } X_{di}^l \text{ THEN } G_s \text{ is } Y_i^l \quad (19)$$

with

$$X_i, X_{di}, G_s = \left[ \text{NB, NM, NS, Z, PS, PM, PB} \right] \quad (20)$$

where $X_i$ and $X_{di}$ are fuzzy set of the input, $G_s$ is fuzzy set of the output. $N'$ and $P$ denote the negative and positive of the membership functions. $i = 1, \ldots, n$. The rule base of T2FS is listed in Table 1.
4. Simulation Results

The proposed grid-connected WTGs in Fig. 1 is verified by using matlab simulink. The proposed WTGs using PMSG 3HP driven by horizontal wind turbine with blade radius 2 m. WTGs are connected to a grid 220V, 50 Hz, with resistive load 1.5 kW. The Simulation parameters listed in appendix. The proposed system are simulated with variable wind speed, as shown in Fig. 7.

![Wind speed graph](image)

**Fig. 7.** Wind speed

The performances of AFSMOC to regulate PMSG speed is shown in Fig. 8. The rotor speed can be regulated at reference speed for all wind speeds, as shown in Fig. 8a. This shows the good performance of AFSMOC to control the rotor speed at optimum TSR, so that the maximum power can be obtained. Figure 8b shows the TSR graph. Wind turbine has the optimum TSR 8.09. Figure 8b shows that the rotor speed can achieve the maximum point at 0.23 seconds.

When the rotor speed is around the optimum point, TSR always under optimum TSR. This is due to the ever-changing wind speed. The reference speed for maximum power point is always changing according to the change of wind speed and always leading from the measured speed. This causes the speed error always be above zero with maximum error 2.3 rpm, as shown in Fig. 8c. However, the rotor speed remains around the maximum point at all wind speed. This is indicated by the low error of TSR. The maximum error of TSR is 0.03, as shown in Fig. 8b. So it can be concluded that the generator can reach the point of maximum power at all wind speeds, despite the extreme changes of wind speed. Figure 7 shows that the wind speed decrease drastically at a time 0.8 seconds and 3 seconds. Vice versa, an increase drastically at a time 2 seconds and 3.8 seconds. The robustness of AFSMOC in controlling the rotor speed has made the rotor speed remains at the maximum power point, despite drastic changes in wind speed.

The robustness of AFSMOC looks from the electromagnetic torque response with low distortion in Fig. 8d, as well as the q-axis stator current in Fig.8e. AFSMOC still able to control the rotor speed at the maximum power point with low distortion of the electro magnetic torque when there is an extreme change of wind speed at time 3 second. This shows that the adaptive gain from T2FS has worked well to improve the robustness of SMC to handle the uncertainty of parameters due disturbances.

![Graphs of various parameters](image)

**Fig. 8.** The performances of AFSMOC. (a) Rotor speed, (b) TSR, (c) rotor speed error, (d) elektro magnetic torque, (e) q-axis stator current

The AFSMOC performances to regulate the rotor speed at maximum power point also can be seen from power coefficient in Fig. 9a, that are always at the maximum point
0.5312 at all wind speeds. Figure 9b shows the power flow from WTGs $P_{con}$ to resistive load. Power flow of WTGs decrease the power supply from the grid $P_{grid}$ to load. The highest power flows from the generator to the load occurs when the wind speed of 8 m/s at time 3 seconds. This indicates that the VSMC are functioning properly.

Figure 9b shows the power flow from WTGs $P_{con}$ to resistive load. Power flow of WTGs decrease the power supply from the grid $P_{grid}$ to load. The highest power flows from the generator to the load occurs when the wind speed of 8 m/s at time 3 seconds. This indicates that the VSMC are functioning properly.

![Figure 9a](image)

**Fig. 9.** (a) power coefficient (b) power (c) generator currents (d) DC-Link voltages results.

The generator side currents in Fig. 9c shows that a VSMC has functioned well as a frequency converter for variable speed control of WTGs. The generator type used is sinusoidal PMSG, so that also produces a sinusoidal current in generator side, as shown in Fig. 9c.

Figure 9d shows that the modulation strategies of CSC stage has produced maximum DC-link voltage so that the maximum voltage transfer ratio can be obtained. Due to the zero-voltage vector cancellation in CSC modulation, the DC-link voltage does not consist of the zero voltage level, as shown in Fig. 9d.

![Figure 10a](image)

**Fig. 10.** (a) grid side voltages (b) THD of voltages, (c) grid side currents, (d) THD of currents
Small LC filter at grid side can reduce harmonics due switching frequency of converter. Both sinusoidal voltage and sinusoidal current at a gridside can be achieved, as shown in Fig. 10a and Fig. 10c. Low harmonic of grid side voltage can be seen in Fig. 10b with THD 0.35%, while the THD of current 6.82%, as shown in Fig. 10d. This indicates that the VSMC has advantages for grid-connected WTGs.

5. Conclusion

Variable speed control of grid-connected PMSG wind turbine using VSMC based on has been discussed. The PMSG speed is controlled by AFSMOC through the $q$-axis stator current control to obtain maximum power at all wind speeds. T2FS is applied in AFSMOC to obtain adaptive gain the sliding mode control, so the robustness of controller can be improved. The advantages of VSMC are it can provide both sinusoidal line voltage and sinusoidal line current, so that the harmonics due switching frequency can be minimized. Simulation results shows that the AFSMOC can regulate the PMSG speed at optimum TSR so that the maximum power can be achieved at all wind speeds. VSMC also provide good performance for improve power quality of WTGs. Low harmonic for both line voltage and line current can be achieved with THD of line voltage with 0.35% and THD of line current 6.82%.

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References


Appendix

**PMSG data**

- Stator resistance \( R_s = 0.2 \Omega \)
- Stator inductance \( L_s = L_d = 8.5 \text{mH} \)
- Pole pair numbers \( n_p = 4 \)
- Flux of permanent magnet \( \psi_m = 0.175 \text{Wb} \)
- Momen of inertia \( J = 0.089 \text{kg m}^2 \)
- Friction coefficient \( B = 0.005 \text{N.m.s/\text{rad}} \)

**Wind Turbine Data**

- Blade radius \( R = 2 \text{m} \)
- Maximum power coefficient \( C_{p,\text{max}} = 0.5312 \)
- Optimum TSR \( \lambda_{\text{opt}} = 8.09 \)